From:	(b) (6)
To:	Moody, Dustin (Fed); Perlner, Ray A. (Fed)
Subject:	ABC
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Hi, guys,

Maybe if we have room in the final version we could put an analysis of an ABC minrank attack using minors modeling. I think that it is interesting to compare the linear algebra search vs the grobner basis techniques.

For quad-abc, you have  $2s^2$  matrices and a target rank of 2s. I haven't calculated the Hilbert Series for the minors ideal, but my guess is that the degree of regularity will be 2s+1. If that is the case, then the asymptotic complexity will be something like  $s^{(2(2s+1)w)}$  where w is the linear algebra constant. So the number of operations over F\_q is independent of q, but this definitely has exponential complexity. If we compare this to our complexity, the break even point should be something very very roughly like q= $s^{(4w)}$ , or basically  $s^9$ . If s=8, then we have q about  $2^{(27)}$ .

The case for cubic is a little worse. You need to randomly select a vector to collapse the 3tensors into a list of  $2s^2$  2-tensors to apply minors modeling. Then you get an extra factor of q to randomly choose a vector in some band kernel. so the complexity should be about  $qs^{(2(2s+1)w)}$ , which is no longer independent of q. The break even point should still be about the same though.

Cheers!